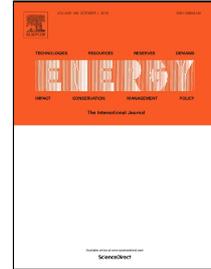


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# 1 A cyber-physical-social system with parallel learning 2 for distributed energy management of a microgrid

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7

8 **Abstract**—A novel cyber-physical-social system (CPSS) with parallel learning is presented for distributed energy  
9 management (DEM) of a microgrid. CPSS is developed by extending the conventional cyber-physical system to the social  
10 space with human participation and interaction. Each energy supplier or each energy demander is regarded as a human  
11 in the social space, who is able to learn the knowledge, co-operate with others, and make a decision with various  
12 preference behaviors. The correlated equilibrium (CE) based general-sum game is employed for realizing the human  
13 interaction on the complex optimization subtask, while the novel adaptive consensus algorithm is used for achieving that  
14 on the simple optimization subtask with multi-energy balance constraints. A real-world system and multiple virtual  
15 artificial systems are introduced for parallel and interactive execution based on the small world network, thus a higher  
16 quality optimum of DEM can be rapidly emerged with a high probability. Case studies of a microgrid with 11 energy  
17 suppliers and 7 energy demanders demonstrate that the proposed technique can effectively achieve the human-computer  
18 collaboration and rapidly obtain a higher quality optimum of DEM compared with other centralized heuristic  
19 algorithms.

20

21 **Keywords** – Cyber-physical-social system; Parallel learning; Correlated equilibrium; Adaptive consensus algorithm;  
22 Distributed energy management

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Nomenclature			
<i>Variables</i>			
$P_{dg}$	electricity energy output of conventional DER	$a^{lin}, b^{lin}$	coefficients of linear demand versus price expression
$H_h$	heat energy output of heat-only unit	$N_{dg}$	number of DG
$P_{chp}$	electricity energy output of CHP unit	$N_h$	number of heat-only units
$H_{chp}$	heat energy output of CHP unit	$N_{chp}$	number of CHP units
$P_{tic}$	tie-line power	$N_{dr}$	number of energy demanders
$\Delta D$	responding power	$N_{wt}$	number of WT
$a_j$	action of the $j$ th agent	$N_{pv}$	number of PV units
$Q_j^k$	the knowledge matrix of the $j$ th agent	$\eta$	maximum allowable power curtailment portion
$\pi_j$	probability distributions of state-action pairs	$\alpha$	knowledge learning factor
$R_j$	feedback reward of the $j$ th agent	$\gamma$	discount factor
$\lambda_p$	incremental cost of the $p$ th agent	$\varepsilon$	exploitation rate
$x_j^k$	solution of the $j$ th agent at the $k$ th iteration	$\mu$	adjustment factor of energy mismatch
$x_p^c$	energy consensus value of the $p$ th agent	$C_1, C_2$	feedback reward coefficients
$x^{ik}$	current solution of the $i$ th VAS	$k_{max}$	maximal iteration number
$x_b^{rk}$	current best solution of the real-world system		
$p_{iw}$	interaction probability between the $i$ th VAS and the $w$ th VAR	<i>Abbreviation</i>	
$h^i$	current best VAS in the $i$ th VAR's interactive network	$s$	
$f_{cost}$	total operating cost	CE	correlated equilibrium
$v$	current wind speed	CPS	cyber-physical system
$S$	current irradiance	CPSS	cyber-physical-social system
$T$	ambient temperature	DERs	distributed energy resources
<i>Parameters</i>		EMS	energy management system
$v_r$	rated wind speed	DEM	distributed energy management
$v_{in}, v_{out}$	cut-in and cut-out wind speeds	RL	reinforcement learning
$\alpha_{pv}$	temperature coefficient	DG	diesel generator
$\alpha_{dg}, \beta_{dg}, \gamma_{dg}$	fuel cost coefficients of conventional DER	VASs	virtual artificial systems
$\alpha_h, \beta_h, \gamma_h$	operating cost coefficients of heat-only unit	WT	wind turbine
$\alpha_{chp}, \beta_{chp}, \gamma_{chp}$	operating cost coefficients of CHP unit	PV	photovoltaic
$\delta_{chp}, \theta_{chp}, \zeta_{chp}$	operating cost coefficients of CHP unit	CHP	combined heat and power
$C_{buy}, C_{sell}$	electricity buying price and selling price	GA	genetic algorithm
		PSO	particle swarm optimization
		ABC	artificial bee colony
		GSO	group search optimizer

## 25 1. Introduction

26 With the fast increasing renewable energy, the energy internet [1] which aims to realize the coordination among various  
27 generations, storage devices, and loads in a wide area by the internet technology, has gained extensive studies in recent years  
28 [2]. At present, energy internet is essentially a tight integration between cyber and physical resources, i.e., an application of  
29 cyber-physical system (CPS) on integrated energy systems [3]. Although CPS [4] can offer many potential benefits to the energy  
30 internet, including faster response, higher control precision, larger scale distributed coordination, and so on, but it almost ignores  
31 the human participation and interaction. In fact, the energy internet is highly coupled with the human and social characteristics  
32 [5], thus CPS may not satisfy different optimal operations of integrated energy systems in some cases, e.g., the demand response  
33 management without considering the social characteristics of different consumers. As a result, the cyber-physical-social system  
34 (CPSS) [6] was developed by logically extending CPS to the social space with human participation and interaction. As a  
35 promising system architecture of industry, CPSS is well available as a core part of future intelligent energy systems [7],

36 rightfully including the multi-energy microgrid.

37 Microgrid is usually a small-scale multi-energy system with a low-voltage distribution network [8], which can effectively  
38 integrate various distributed energy resources (DERs), storage devices, and controllable loads in the grid-connected or islanded  
39 mode. In general, energy management of a microgrid seeks to minimize the total operating cost via an optimal dispatch strategy  
40 of energy balance among DERs, storage devices, tie-line power from the main grid, and controllable loads under various  
41 constraints [9]. In order to address this problem, the centralized optimization is the most commonly used type of methods, e.g.,  
42 mixed integer linear programming [10] and gravitational search algorithm [11], which often produce a satisfactory result with a  
43 low total operating cost. However, it easily leads to a communication bottleneck in a microgrid with a larger number of  
44 controllable devices since the centralized energy management systems (EMS) needs to collect and process all the corresponding  
45 information from each one, which also cannot ensure the security and privacy of each owner [12]. In terms of the optimization  
46 performance, the centralized optimizer is apt to trap in a relatively high computation burden or a low-quality optimum with the  
47 great increasing controllable devices. Furthermore, it cannot satisfy the requirement of high operation reliability because the  
48 operation of an entire microgrid completely depends on the only centralized optimizer.

49 For the sake of handling these issues, the distributed control architecture is more suitable for the practical energy  
50 management [13], thus various distributed optimization algorithms have been proposed for distributed energy management  
51 (DEM) of a microgrid. The consensus algorithms have been deeply researched for DEM due to its remarkable self-organizing  
52 ability, significant robustness, and easy scalability [14]-[16], in which the performance influence by the time delays in  
53 communication network is strictly investigated in [17]. Besides, the sub-gradient based distributed optimization was also  
54 successfully designed for minimizing the total operating cost of a microgrid [18],[19]. In order to effectively realize the complex  
55 interaction among independent agents [20], the game theory, e.g., Stackelberg game [21] and bargaining game [22], were  
56 introduced to combine different optimization techniques for DEM. Unfortunately, all of these algorithms mainly suffer from the  
57 following four problems:

58 ●*High dependence on the mathematical model*: The core optimizers are essentially the gradient-based algorithms, the  
59 performance of which are fully determined by the initial solution of DEM. Therefore, it easily leads to a low quality local-  
60 optimum if nonlinearities, nonconvexity, discontinuous and nondifferentiable objective functions (e.g., purchase energy cost or  
61 sell energy benefit according to direction of tie-line power), and complex constraints (e.g., the heat-power feasible operation  
62 region of combined heat and power (CHP) units [23]) exist.

63 ●*Incapability of knowledge learning and single decision strategy*: Each game agent is constructed with only a single  
64 decision strategy and is incapable of knowledge learning, which is not consistent with the intelligent human in real-world  
65 system.

66     ●*Invalid multi-energy interactions with consensus algorithm*: The consensus based human interaction is only suitable for  
 67 only single energy interaction among the local energy supplier and demander, which cannot satisfy the multi-energy interaction  
 68 with multiple energy balance constraints.

69     ●*Inefficient optimization with a single execution system*: The traditional game theory based human interaction usually seeks  
 70 an optimal equilibrium with a single execution system, which easily results in a long computation time as the iterations may  
 71 involve repeated games.

72     In order to simultaneously address these problems, this paper proposes a CPSS with parallel learning for DEM of a  
 73 microgrid, which has the following features and novelties:

- 74     ● CPSS is firstly introduced to DEM of a microgrid, which fully considers the human (energy supplier or energy demander)  
 75 participation and interaction, thus the obtained dispatch strategy is more practical for an optimal operation.
- 76     ● The model-free Q-learning can effectively enable each agent to flexibly handle the nonconvex nonlinear DEM with  
 77 complex constraints and nondifferentiable objective functions, while each agent can learn the knowledge from the  
 78 continuous interactions with the environment. Instead of a single decision strategy, the correlated equilibrium (CE) based  
 79 general-sum game [24] with multiple decision strategies is used for increasing the decision diversity of each human.
- 80     ● By improving the original consensus algorithm, the adaptive consensus algorithm is proposed for effectively achieving the  
 81 multi-energy interactions with multiple energy balance constraints, thus they can reach a consensus (optimum) on the  
 82 incremental cost.
- 83     ● Multiple virtual artificial systems (VASs) are built to guide the real-world system for DEM with a single execution system,  
 84 thus the game interaction efficiency of the real-world system can be dramatically improved without any adverse trials  
 85 according to the guidance by all the VASs. Besides, the small world network is adopted for constructing the interaction  
 86 network among different VASs, which can properly balance the exploitation and exploration of VASs.

87     The remaining of this paper is organized as follows. Section 2 presents the mathematical model of DEM of a microgrid.  
 88 Section 3 gives the design of CPSS with parallel learning for DEM. Case studies are carried out in Section 4. Finally, Section 5  
 89 concludes the paper.

## 90     **2. Mathematical model of DEM of a microgrid**

91     Traditionally, a microgrid adopts the centralized energy management for an optimal operation under different scenarios. It  
 92 aims to determine the optimal dispatch scheme for all the energy suppliers or demanders via a centralized optimizer. In contrast,  
 93 The proposed DEM allows each energy supplier or demander to calculate its own optimal energy output or demand via a  
 94 coordination with interactive agents. Moreover, the primary task of DEM is to achieve the energy balance between the supply

95 and demand, as shown in Fig. 1. In general, the supply side can consist of various energy suppliers, including wind turbine  
 96 (WT), photovoltaic (PV) unit, CHP unit, diesel generator (DG), and so on. On the other hand, the demand side usually contains  
 97 three types of energy demanders, i.e., residential building, factory, and commercial building.

## 98 2.1. Energy suppliers

99 (i) *Renewable energy resources*: for improving the generation power outputs of renewable energy resources, both WT and  
 100 PV unit are operated at the maximum power points under different weather conditions, which can be expressed as follows  
 101 [25],[26]:

$$102 \quad P_{wt} = \begin{cases} 0, & \text{for } v < v_{in} \text{ and } v > v_{out} \\ P_{wt}^r \frac{v - v_{in}}{v_r - v_{in}}, & \text{for } v_{in} \leq v \leq v_r \\ P_{wt}^r, & \text{for } v_r < v \leq v_{out} \end{cases} \quad (1)$$

$$103 \quad P_{pv} = P_{pv}^r \left( 1 + \alpha_{pv} \cdot (T - T_{ref}) \right) \cdot \frac{S}{S_{ref}} \quad (2)$$

104 where  $P_{wt}$  and  $P_{pv}$  are the current maximum power points of WT and PV unit, respectively;  $P_{wt}^r$  and  $P_{pv}^r$  are the rated power of  
 105 WT and PV unit, respectively;  $v_r$  is the rated wind speed;  $v$  is the current wind speed;  $v_{in}$  and  $v_{out}$  are the cut-in and cut-out wind  
 106 speeds, respectively;  $S$  is the current irradiance;  $S_{ref}$  is the reference irradiance;  $T$  is the ambient temperature;  $T_{ref}$  is the reference  
 107 temperature; and  $\alpha_{pv}$  is the temperature coefficient.

108 (ii) *Conventional DER*: this type of suppliers is essentially a dispatchable synchronous generator, e.g., diesel or natural gas  
 109 generators, which can easily regulate its electricity energy output. In general, the fuel cost of the conventional DER can be  
 110 expressed via a typical quadratic function, as follows [27]:

$$111 \quad f_{dg} (P_{dg}) = \alpha_{dg} + \beta_{dg} P_{dg} + \gamma_{dg} P_{dg}^2 \quad (3)$$

112 where  $P_{dg}$  is the electricity energy output of conventional DER;  $\alpha_{dg}$ ,  $\beta_{dg}$ , and  $\gamma_{dg}$  are the fuel cost coefficients of conventional  
 113 DER.

114 (iii) *Heat-only unit*: such as gas furnace or heater exchanger, it can only provide the heat energy for local demanders in a  
 115 microgrid. Similarly, its operating cost can be constructed as a quadratic function, as follows [27]:

$$116 \quad f_h (H_h) = \alpha_h + \beta_h H_h + \gamma_h H_h^2 \quad (4)$$

117 where  $H_h$  is the heat energy output of heat-only unit;  $\alpha_h$ ,  $\beta_h$ , and  $\gamma_h$  are the operating cost coefficients of heat-only unit.

118 (iv) *CHP unit*: as a co-generation unit, it can significantly increase the thermal efficiency and reduce the environment  
 119 emissions [28] by reusing the heat, thus both the electricity and heat energy can be simultaneously generated, where the total  
 120 operating cost can be calculated as follows [29]:

$$f_{\text{chp}}(P_{\text{chp}}, H_{\text{chp}}) = \alpha_{\text{chp}} + \beta_{\text{chp}} P_{\text{chp}} + \gamma_{\text{chp}} P_{\text{chp}}^2 + \delta_{\text{chp}} H_{\text{chp}} + \theta_{\text{chp}} H_{\text{chp}}^2 + \xi_{\text{chp}} H_{\text{chp}} P_{\text{chp}} \quad (5)$$

where  $P_{\text{chp}}$  is the electricity energy output of CHP unit;  $H_{\text{chp}}$  is the heat energy output of CHP unit;  $\alpha_{\text{chp}}$ ,  $\beta_{\text{chp}}$ ,  $\gamma_{\text{chp}}$ ,  $\delta_{\text{chp}}$ ,  $\theta_{\text{chp}}$ , and  $\xi_{\text{chp}}$  are the operating cost coefficients of CHP unit.

(v) *Main grid*: when the microgrid is operated in the grid-connected mode, the main grid can be regarded as an electricity energy supplier if the total electricity energy output of all the DERs is insufficient to balance the total electricity energy demand of all the loads in the microgrid, otherwise it will become an electricity energy demander. Hence, the operating cost from the main grid can be determine by the direction of tie-line power and the current electricity price, as follows:

$$f_{\text{mg}}(P_{\text{tie}}) = \begin{cases} C_{\text{buy}} P_{\text{tie}}, & \text{if } P_{\text{tie}} \geq 0 \\ C_{\text{sell}} P_{\text{tie}}, & \text{otherwise} \end{cases} \quad (6)$$

where  $C_{\text{buy}}$  and  $C_{\text{sell}}$  are the electricity buying price and selling price, respectively; and  $P_{\text{tie}}$  is the tie-line power, while a negative  $P_{\text{tie}}$  will result in a negative operating cost, i.e., the electricity selling profit from the microgrid to the main grid.

## 2.2. Energy demanders

In order to reduce the peak-valley difference of total power load for an electric power system, the electricity company generally employs a time-of-use pricing strategy to allow the demanders to automatically adjust their electric power consumptions. In general, this process is well known as demand response (DR). Based on the linear demand versus price expression [30], the cost function of each energy demander can be calculated according to the responding power (power curtailment) and his or her sensitiveness of power loads, as follows:

$$f_{\text{dr}}(\Delta D) = \frac{-1}{b^{\text{lin}}} \Delta D^2 + \frac{D_0 - a^{\text{lin}}}{b^{\text{lin}}} \Delta D \quad (7)$$

where  $\Delta D$  is the responding power;  $D_0$  is the current initial electric power;  $a^{\text{lin}}$  and  $b^{\text{lin}}$  are the coefficients of linear demand versus price expression.

## 2.3. Social welfare and constraints

In this paper, DEM aims to maximize the social welfare (i.e., minimize the total operating cost) of the microgrid while satisfying all the constraints, including energy balance constraint, capacity limits of all energy sources, feasible operating region constraints of CHP units, and minimum demand constraint of each energy demander for the must-run loads. Hence, the mathematical model of DEM of a microgrid can be described as follows [19]:

$$\min f_{\text{cost}} = \sum_{i=1}^{N_{\text{dg}}} f_{\text{dg}}^i(P_{\text{dg}}^i) + \sum_{j=1}^{N_{\text{h}}} f_{\text{h}}^j(H_{\text{h}}^j) + \sum_{k=1}^{N_{\text{chp}}} f_{\text{chp}}^k(P_{\text{chp}}^k, H_{\text{chp}}^k) + \sum_{m=1}^{N_{\text{dr}}} f_{\text{dr}}^m(\Delta D^m) + f_{\text{mg}}(P_{\text{tie}}) \quad (8)$$

subject to

$$147 \quad \sum_{i=1}^{N_{\text{dg}}} P_{\text{dg}}^i + \sum_{k=1}^{N_{\text{chp}}} P_{\text{chp}}^k + \sum_{l=1}^{N_{\text{wt}}} P_{\text{wt}}^l + \sum_{d=1}^{N_{\text{pv}}} P_{\text{pv}}^d + P_{\text{tie}} - \sum_{m=1}^{N_{\text{dr}}} \Delta D^m = 0 \quad (9)$$

$$148 \quad \sum_{j=1}^{N_{\text{h}}} H_{\text{h}}^j + \sum_{k=1}^{N_{\text{chp}}} H_{\text{chp}}^k - H_{\text{demand}} = 0 \quad (10)$$

$$149 \quad P_{\text{dg}}^{i,\min} \leq P_{\text{dg}}^i \leq P_{\text{dg}}^{i,\max}, \quad i = 1, 2, \dots, N_{\text{dg}} \quad (11)$$

$$150 \quad H_{\text{h}}^{j,\min} \leq H_{\text{h}}^j \leq H_{\text{h}}^{j,\max}, \quad j = 1, 2, \dots, N_{\text{h}} \quad (12)$$

$$151 \quad P_{\text{chp}}^{k,\min}(H_{\text{chp}}^k) \leq P_{\text{chp}}^k \leq P_{\text{chp}}^{k,\max}(H_{\text{chp}}^k), \quad k = 1, 2, \dots, N_{\text{chp}} \quad (13)$$

$$152 \quad H_{\text{chp}}^{k,\min}(P_{\text{chp}}^k) \leq H_{\text{chp}}^k \leq H_{\text{chp}}^{k,\max}(P_{\text{chp}}^k), \quad k = 1, 2, \dots, N_{\text{chp}} \quad (14)$$

$$153 \quad P_{\text{tie}}^{\min} \leq P_{\text{tie}} \leq P_{\text{tie}}^{\max} \quad (15)$$

$$154 \quad 0 \leq \Delta D^m \leq \eta D_0^m, \quad m = 1, 2, \dots, N_{\text{dr}} \quad (16)$$

155 where the superscripts  $i, j, k, m, l$ , and  $d$  represent the  $i$ th DG, the  $j$ th heat-only unit, the  $k$ th CHP unit, the  $m$ th energy demander,  
 156 the  $l$ th WT, and the  $d$ th PV unit, respectively; the superscripts  $min$  and  $max$  represent the lower and upper limits, respectively;  
 157  $N_{\text{dg}}$  is the number of DG;  $N_{\text{h}}$  is the number of heat-only units;  $N_{\text{chp}}$  is the number of CHP units;  $N_{\text{dr}}$  is the number of energy  
 158 demanders;  $N_{\text{wt}}$  is the number of WT;  $N_{\text{pv}}$  is the number of PV units; and  $\eta$  denotes the maximum allowable power curtailment  
 159 portion of the current initial electric power, which can ensure the normal operation of must-run loads for the energy demanders.

160 Since both WT and PV units are operated at the maximum power points under different weather conditions [31], their  
 161 maintenance costs are fixed for each optimization task. Hence, the operating costs of WT and PV unit are not considered in the  
 162 total operating cost  $f_{\text{cost}}$  due to their inherent zero fuel consumption. Moreover, the feasible operating region constraints of CHP  
 163 units (13) and (14) indicate that the electricity energy output and heat energy output are tightly coupled. In general, the shape of  
 164 the feasible operating region is mainly determined by the struct of CHP units, e.g., the primary mover. It usually consists of two  
 165 types, including one segment shape and two segment shape [32], as illustrated in Fig. 2. In fact, both of them belong to convex  
 166 and nonconvex feasible operating regions, respectively. For example, the back-pressure CHP unit with condensing and auxiliary  
 167 cooling options, gas turbines, and combined gas and steam cycles can result in the nonconvex feasible operating region [33]. It  
 168 can be observed from Fig. 2 that the energy outputs of CHP units should be enclosed by the boundary curves ABCD or  
 169 ABCDEF [23], where both the lower and upper limits of electricity energy output are determined by different heat energy  
 170 outputs and vice versa. In order to reduce the optimization difficulty, DEM of a microgrid is decomposed into two optimization  
 171 subtasks. The first one is responsible for optimizing the tie-line power and the heat energy outputs of CHP units, which is  
 172 relatively complex with a nondifferentiable operating cost from the main grid (6) and the feasible operating region constraints.  
 173 Based on the decision results of the first optimization subtasks, the second one with the rest of operating cost and constraints is

174 essentially a convex optimization and relatively easy to be addressed.

### 175 **3. CPSS with parallel learning for DEM**

#### 176 *3.1. CPSS framework for DEM of a microgrid*

177 As illustrated in Fig. 3, CPSS is a complex system with three dimensions, including physical space, cyberspace, and social  
178 space, and all of them are tightly connected via the cyberspace [6]. For DEM of a microgrid, the main task of CPSS is to  
179 maximize the social welfare and to react to the physical space. Compared with CPS, the major improvement part of CPSS is the  
180 social space with human beings, such as human behaviors and human interactions. For each optimization task, each energy  
181 supplier or energy demander firstly acquires current operating parameters of the corresponding distributed device from the  
182 physical space, then each of them will autonomously make a dispatch decision through the interaction with others in social space  
183 based on the communication and computation in cyberspace with parallel learning, finally the optimal dispatch strategy will be  
184 issued to each distributed device for optimal control in the physical space.

185 For effectively searching a high quality dispatch strategy, a CE based general-sum game with model-free Q-learning [24] is  
186 used for achieving the human interaction on the complex optimization subtask, while the novel adaptive consensus algorithm is  
187 implemented for human interaction on the simple optimization subtask.

#### 188 *3.2. Parallel learning with multiple parallel systems*

189 According to the real-world system, multiple parallel VASs [34] are constructed for different evolutions of DEM in a  
190 microgrid. In this paper, the real-world system mainly provides the optimization model (8)-(16), the current best solution, and  
191 the energy management knowledge of each agent to multiple VASs, then each VAS can generate an optimal dispatch strategy  
192 via the human interactions and risk-free trial-and-error, while the energy management knowledge of each agent will be updated.  
193 Consequently, the parallel  $n$ -VASs will vote for  $n$  optimal dispatch strategies and provide their energy management knowledge  
194 to the real-world system, while each VAS will improve its dispatch strategy and energy management knowledge through  
195 learning from its interactive VASs based on small world network, as shown in Fig. 4.

##### 196 *3.2.1 CE based human interaction on complex optimization subtask*

###### 197 *(i) CE based general-sum game*

198 For a general-sum game, a CE is more general than a Nash equilibrium as the set of Nash equilibria is wholly included in the  
199 set of correlated equilibria [24]. Generally speaking, a CE is a probability distribution of joint actions from which no agent is  
200 motivated to deviate unilaterally, which can be combined with Q-learning, as follows:

$$201 \quad \left\{ \begin{array}{l} \sum_{\bar{a}_{-j} \in \mathcal{A}_{-j}(s_k)} \boldsymbol{\pi}_j(s_k, \bar{a}) \boldsymbol{Q}_j^k(s_k, (\bar{a}_{-j}, a_j)) \geq \sum_{\bar{a}_{-j} \in \mathcal{A}_{-j}(s_k)} \boldsymbol{\pi}_j(s_k, \bar{a}) \boldsymbol{Q}_j^k(s_k, (\bar{a}_{-j}, a_j^o)) \\ \mathcal{A}_{-j} = \prod_{p \neq j} \mathcal{A}_p, \bar{a}_{-j} = \prod_{p \neq j} a_p, \bar{a} = (\bar{a}_{-j}, a_j), a_j^o \neq a_j \end{array} \right. \quad (17)$$

202 where  $\boldsymbol{\pi}_j$  is the probability distributions of state-action pairs of the  $j$ th agent, which can be called a CE when it satisfies the  
 203 inequality constraint (17);  $\boldsymbol{Q}_j^k$  is the knowledge matrix of the  $j$ th agent at the  $k$ th iteration, which represent the knowledge values  
 204 of station action pairs;  $s_k$  is the state of the multi-agent system at the  $k$ th iteration;  $\bar{a} = [a_1, \dots, a_j, \dots, a_J]$  is the joint action of all  
 205 the agents;  $a_j$  is the action of the  $j$ th agent;  $J$  is the number of agents;  $\bar{a}_{-j}$  is the joint action of all the agents except the  $j$ th agent;  
 206  $\mathcal{A}(s_k)$  is the agents' set of available joint actions in state  $s_k$ ;  $\mathcal{A}_j$  is the  $j$ th agent's set of pure actions; and  $a_j^o$  is the  $j$ th agent's any  
 207 other action except  $a_j$ .

### 208 (ii) Knowledge learning

209 According to the state-action-reward-state data via continuous interactions with the environment, each agent can update its  
 210 own knowledge of different state-action pairs with the feedback rewards by reinforcement learning. In this paper, Q-learning is  
 211 used for achieving this learning process, thus the knowledge can be stored by the Q-value matrix, as follows [35]:

$$212 \quad V_j(s_{k+1}) = \sum_{\bar{a} \in \mathcal{A}(s_{k+1})} \boldsymbol{\pi}_j(s_{k+1}, \bar{a}) \boldsymbol{Q}_j^k(s_{k+1}, \bar{a}) \quad (18)$$

$$213 \quad \boldsymbol{Q}_j^{k+1}(s_k, \bar{a}) = \boldsymbol{Q}_j^k(s_k, \bar{a}) + \alpha [(1-\gamma)R_j(s_k, \bar{a}) + \gamma V_j(s_{k+1}) - \boldsymbol{Q}_j^k(s_k, \bar{a})] \quad (19)$$

214 where  $V_j(s_{k+1})$  denotes the state value-function of the  $j$ th agent for state  $s_{k+1}$ ;  $\alpha$  is the knowledge learning factor;  $\gamma$  is the discount  
 215 factor; and  $R_j(s_k, \bar{a})$  is the feedback reward after implementing a joint action  $\bar{a}$  at the state  $s_k$ .

### 216 (iii) Decision strategies

217 In the complex optimization subtask, the strategy decision of each agent is divided into two processes. Firstly, each agent  
 218 choose a pure action strategy (i.e., interval of optimization) according to its preference behavior, then an accurate solution can be  
 219 determined by the non-uniform mutation operator based on the local optimum of the corresponding interval. In this paper, four  
 220 human decision strategies are introduced to each agent for selecting a pure action, as [24]

- 221 • *Utilitarian behavior*: maximize the sum of all agents' benefits, as follows:

$$222 \quad \max f_b(\boldsymbol{\pi}_j) = \sum_{j=1,2,\dots,J} \sum_{\bar{a} \in \mathcal{A}(s_k)} \boldsymbol{\pi}_j(s_k, \bar{a}) \boldsymbol{Q}_j^k(s_k, \bar{a}) \quad (20)$$

- 223 • *Egalitarian behavior*: maximize the minimum of all agents' benefits, as follows:

$$224 \quad \max f_b(\boldsymbol{\pi}_j) = \min_{j=1,2,\dots,J} \sum_{\bar{a} \in \mathcal{A}(s_k)} \boldsymbol{\pi}_j(s_k, \bar{a}) \boldsymbol{Q}_j^k(s_k, \bar{a}) \quad (21)$$

- 225 • *Plutocratic behavior*: maximize the maximum of all agents' benefits, as follows:

$$226 \quad \max f_b(\boldsymbol{\pi}_j) = \max_{j=1,2,\dots,J} \sum_{\bar{a} \in \mathcal{A}(s_k)} \boldsymbol{\pi}_j(s_k, \bar{a}) \boldsymbol{Q}_j^k(s_k, \bar{a}) \quad (22)$$

227 • *Dictatorial behavior*: maximize the maximum of any individual agent's benefits, as follows:

$$228 \quad \max f_b(\boldsymbol{\pi}_j) = \sum_{\bar{a} \in \mathcal{A}(s_k)} \boldsymbol{\pi}_j(s_k, \bar{a}) \mathcal{Q}_j^k(s_k, \bar{a}) \quad (23)$$

229 where  $f_b$  is the behavior function, in which the maximum and the corresponding optimal CE can be calculated by linear  
230 programming with the inequality constraints (17) and the following constraints, as

$$231 \quad \sum_{\bar{a} \in \mathcal{A}(s_k)} \boldsymbol{\pi}_j(s_k, \bar{a}) = 1, \quad 0 \leq \boldsymbol{\pi}_j(s_k, \bar{a}) \leq 1 \quad (24)$$

232 After acquiring the optimal CE  $\boldsymbol{\pi}_j^*$ , a pure action of each agent and an accurate dispatch strategy can be determined. Aiming  
233 at a proper trade-off between exploration and exploitation, the  $\varepsilon$ -Greedy rule [36] is used for interval selection, as

$$234 \quad a_j = \begin{cases} \arg \max_{a_j \in \mathcal{A}_j} \boldsymbol{\pi}_j(s_k, (a_{-j}, a_j)), & \text{if } q_0 \leq \varepsilon \\ a_{\text{rand}}, & \text{otherwise} \end{cases} \quad (25)$$

$$235 \quad x_j^k = \begin{cases} x_j^{\text{best}}(a_j) + \Delta[k, x_j^{\text{ub}}(a_j) - x_j^{\text{best}}(a_j)], & \text{if } \text{rand}(0,1) < 0.5 \\ x_j^{\text{best}}(a_j) - \Delta[k, x_j^{\text{best}}(a_j) - x_j^{\text{lb}}(a_j)], & \text{otherwise} \end{cases} \quad (26)$$

$$236 \quad \begin{cases} x_j^{\text{ub}}(a_j) = x_j^{\text{min}} + a_j \cdot (x_j^{\text{max}} - x_j^{\text{min}}) / |\mathcal{A}_j| \\ x_j^{\text{lb}}(a_j) = x_j^{\text{min}} + (a_j - 1) \cdot (x_j^{\text{max}} - x_j^{\text{min}}) / |\mathcal{A}_j| \end{cases} \quad (27)$$

$$237 \quad \Delta[k, y] = y \cdot \left(1 - r^{(1-k/k_{\text{max}})^b}\right) \quad (28)$$

238 where  $q_0$  is a uniform random value from  $[0, 1]$ ;  $\varepsilon$  is the exploitation rate which represents the probability of exploitation;  $a_{\text{rand}}$   
239 denotes a random action (exploration) chosen from the action space  $\mathcal{A}_j$ ;  $x_j^{\text{best}}(a_j)$  is the previous best optimal solution at the action  
240  $(a_j)$  interval of the  $j$ th controllable variable;  $x_j^{\text{ub}}(a_j)$  and  $x_j^{\text{lb}}(a_j)$  are the upper and lower bounds of the action  $(a_j)$  interval,  
241 respectively;  $x_j^{\text{min}}$  and  $x_j^{\text{max}}$  are the minimum and maximum values of the  $j$ th controllable variable, respectively;  $\Delta[k, y]$  is a  
242 decay function as the iteration  $k$  increases;  $r$  is a uniform random value from  $[0, 1]$ ;  $b$  is the system parameter which determines  
243 the degree of non-uniformity; and  $k_{\text{max}}$  is the maximal iteration number.

### 244 3.2.2 Adaptive consensus algorithm based human interaction on simple optimization subtask

#### 245 (i) Graph theory of interaction network

246 The interaction network among humans can be typically built with a directed graph  $G=(V, E, A)$ , where  $V=\{v_1, v_2, \dots, v_N\}$  is  
247 the set of nodes (agents);  $E \subseteq V \times V$  denotes the edges (interactions); and  $A=[a_{pq}] \in R^{N \times N}$  is a weighted adjacency matrix [37].  
248 Based on these most basic elements, the Laplacian matrix  $L=[l_{pq}] \in R^{N \times N}$  and row stochastic matrix  $D=[d_{pq}] \in R^{N \times N}$  of the graph  $G$   
249 can be calculated as follows:

$$250 \quad l_{pp} = \sum_{p=1, q \neq p}^N a_{pq}, l_{pq} = -a_{pq}, \forall p \neq q \quad (29)$$

$$d_{pq}[k] = |l_{pq}| / \sum_{q=1}^N |l_{pq}|, \quad p = 1, 2, \dots, N \quad (30)$$

(ii) *Adaptive consensus algorithm on incremental cost*

The adaptive consensus algorithm inherently represents a herd behavior of human interactions, i.e., each agent will regulate its own state to reach a consensus with the adjacent agents after acquiring their current states. In this paper, the first-order adaptive consensus algorithm is adopted for this consensus process, as follows [38]:

$$s_p[k+1] = \sum_{q=1}^N d_{pq}[k] s_q[k] \quad (31)$$

where  $s_p$  is the state of the  $p$ th agent.

Note that the simple optimization subtask only has a unique minimum point as it is a strictly convex optimization, thus its global optimum can be obtained when all the agents can reach a consensus on the incremental cost while satisfying various constraints. Hence, the incremental cost is taken as the consensus state for human interactions, which can be written as [14]

$$\lambda_p = \frac{\partial f_p(x_p)}{\partial x_p} = \kappa_p x_p + \varphi_p \quad (32)$$

where  $\lambda_p$  is the incremental cost of the  $p$ th agent;  $x_p$  is the controllable variable (energy output or demand) of the  $p$ th agent;  $\kappa_p$  and  $\varphi_p$  are the incremental cost coefficients of the  $p$ th agent, respectively, which can be determined by the corresponding cost coefficients; and  $f_p$  is the operating cost of the  $p$ th agent.

In order to satisfy the energy balance constraints (9)-(10), the electricity energy mismatch  $\Delta E$  and heat energy mismatch  $\Delta H$  between the energy suppliers and energy demanders are introduced in adaptive consensus algorithm, as follows:

$$\Delta E = \sum_{i=1}^{N_{dg}} P_{dg}^i + \sum_{k=1}^{N_{chp}} P_{chp}^k + \sum_{l=1}^{N_{wt}} P_{wt}^l + \sum_{d=1}^{N_{pv}} P_{pv}^d + P_{tie} - \sum_{m=1}^{N_{dr}} \Delta D^m \quad (33)$$

$$\Delta H = \sum_{j=1}^{N_h} H_h^j + \sum_{k=1}^{N_{chp}} H_{chp}^k - H_{demand} \quad (34)$$

It can be found from (32) that an increasing incremental cost will lead to an increasing energy output and an decreasing energy demand, thus the consensus interaction should be carefully designed to satisfy the energy balance constraints following this changing rule, as follows:

- *Unified consensus*: if the signs of  $\Delta E$  and  $\Delta H$  are consistent, i.e.,  $\Delta E \cdot \Delta H \geq 0$ , then all the agents can update their incremental cost state in an unified interaction network, as

$$\lambda_p[k+1] = \begin{cases} \sum_{q=1}^N d_{pq}[k] \lambda_q[k] - \mu \Delta E, & p \in \Omega_E \\ \sum_{q=1}^N d_{pq}[k] \lambda_q[k] - \mu \Delta H, & p \in \Omega_H \end{cases} \quad (35)$$

- 275 • *Independent consensus*: if the signs of  $\Delta E$  and  $\Delta H$  are inconsistent, i.e.,  $\Delta E \cdot \Delta H < 0$ , then the electricity agents and heat agents  
276 need to be separated to update their incremental cost state in two independent interaction network, as

$$277 \lambda_p[k+1] = \begin{cases} \sum_{q \in \Omega_E} d_{pq}^E[k] \lambda_q[k] - \mu \Delta E, & p \in \Omega_E \\ \sum_{q \in \Omega_H} d_{pq}^H[k] \lambda_q[k] - \mu \Delta H, & p \in \Omega_H \end{cases} \quad (36)$$

278 where  $\Omega_E$  and  $\Omega_H$  represent the sets of electricity agents and heat agents, respectively;  $d_{pq}^E$  is the  $(p,q)$  entry of the row stochastic  
279 matrix of the interaction network among the electricity agents;  $d_{pq}^H$  is the  $(p,q)$  entry of the row stochastic matrix of the  
280 interaction network among the heat agents; and  $\mu$  denotes the adjustment factor of energy mismatch,  $\mu > 0$ .

281 Therefore, each agent will regulate its incremental cost between these two consensus mode according to the sign of  $(\Delta E \cdot \Delta H)$ ,  
282 as illustrated in Fig. 5.

283 By fully considering the lower and upper limits of each controllable variable (11)-(16), the energy output or demand of each  
284 agent can be determined based on (32), as follows [14]:

$$285 x_p^c = \frac{\lambda_p[k] - \varphi_p}{\kappa_p} \quad (37)$$

$$286 x_p^k = \begin{cases} x_p^{\min}, & \text{if } x_p^c < x_p^{\min} \\ x_p^c, & \text{if } x_p^{\min} \leq x_p^c \leq x_p^{\max} \\ x_p^{\max}, & \text{if } x_p^c > x_p^{\max} \end{cases} \quad (38)$$

287 where  $x_p^c$  denotes the energy consensus value of the  $p$ th agent;  $x_p^{\min}$  and  $x_p^{\max}$  are the minimum and maximum values of the  $p$ th  
288 controllable variable, respectively.

### 289 3.2.3 Interaction between different parallel systems

#### 290 (i) Interaction between VASs and the real-world system

291 In the initial phase, the real-world system will provide the prior energy management knowledge  $\mathbf{Q}_j^{p*}$  ( $j=1,2,\dots,J$ ) and the  
292 optimal incremental cost  $\lambda^*$  of a similar optimization task to each VAS, which can be regarded as the initial knowledge matrices  
293  $\mathbf{Q}_j^{j^0}$  and the initial incremental cost  $\lambda$  of each agent. On the other hand, the agent of real-world system will update its current best  
294 solution and the knowledge matrix according to the current solutions of VASs, as follows:

$$295 h = \arg \min_{i=1,2,\dots,n} f_{\text{cost}}(\mathbf{x}^{ik}) \quad (39)$$

$$296 \mathbf{x}_b^{rk} = \begin{cases} \mathbf{x}^{hk}, & \text{if } f_{\text{cost}}(\mathbf{x}_b^{rk}) \geq f_{\text{cost}}(\mathbf{x}^{hk}) \\ \mathbf{x}_b^{rk}, & \text{otherwise} \end{cases} \quad (40)$$

$$297 \mathbf{Q}_j^{rk} = \begin{cases} \mathbf{Q}_j^{rk} + r_Q \cdot (\mathbf{Q}_j^{hk} - \mathbf{Q}_j^{rk}), & \text{if } f_{\text{cost}}(\mathbf{x}_b^{rk}) \geq f_{\text{cost}}(\mathbf{x}^{hk}) \\ \mathbf{Q}_j^{rk}, & \text{otherwise} \end{cases} \quad (41)$$

298 where  $\mathbf{x}^{ik}$  represent the current solution of the  $i$ th VAS, which consists of all the controllable variables;  $h$  denotes the current best  
 299 VAS with the smallest total operating cost;  $\mathbf{x}_b^{rk}$  is the current best solution of the real-world system;  $r_Q$  is the random matrix  
 300 from  $[0,1]$  with the same scale of knowledge matrix; and  $\mathbf{Q}_j^{rk}$  is the current knowledge matrix of the  $j$ th agent in the real-world  
 301 system.

### 302 (ii) Interaction among VASs

303 Generally speaking, the larger otherness between different VASs will lead to more diverse dispatch strategies, which can  
 304 effectively avoid the low-quality local optimum, but it will consume more computation time to search the potential global  
 305 optimum. To properly balance them, the small world network is used for constructing the interaction network among VASs, in  
 306 which each VAS can stochastically interact with any other VASs with a decreasing probability, as follows [39]:

$$307 \quad \rho_{iw} = \left(1 - \frac{k}{k_{\max}}\right) \cdot C_p, \quad w = 1, 2, \dots, n \quad (42)$$

308 where  $\rho_{iw}$  is the interaction probability between the  $i$ th VAS and the  $w$ th VAR;  $k_{\max}$  is the maximal iteration number; and  $C_p$  is  
 309 the probability coefficient, with  $0 < C_p < 1$ .

310 Similarly, each VAS will update its current best solution and the knowledge matrix according to the current solutions of its  
 311 interactive VASs, as follows:

$$312 \quad h^i = \arg \min_{w \in \Omega_i} f_{\text{cost}}(\mathbf{x}^{wk}) \quad (43)$$

$$313 \quad \mathbf{x}_b^{ik} = \begin{cases} \mathbf{x}^{h^i k}, & \text{if } f_{\text{cost}}(\mathbf{x}_b^{ik}) \geq f_{\text{cost}}(\mathbf{x}^{h^i k}) \\ \mathbf{x}_b^{ik}, & \text{otherwise} \end{cases} \quad (44)$$

$$314 \quad \mathbf{Q}_j^{ik} = \begin{cases} \mathbf{Q}_j^{ik} + r_Q \cdot (\mathbf{Q}_j^{h^i k} - \mathbf{Q}_j^{ik}), & \text{if } f_{\text{cost}}(\mathbf{x}_b^{ik}) \geq f_{\text{cost}}(\mathbf{x}^{h^i k}) \\ \mathbf{Q}_j^{ik}, & \text{otherwise} \end{cases} \quad (45)$$

315 where  $h^i$  denotes the current best VAS in the  $i$ th VAR's interactive network;  $\Omega_i$  is the VAR set in the  $i$ th VAS's interactive  
 316 network, which can be determined by (42);  $\mathbf{x}_b^{ik}$  is the current best solution of the  $i$ th VAS; and  $\mathbf{Q}_j^{ik}$  is the current knowledge  
 317 matrix of the  $j$ th agent in the  $i$ th VAS.

## 318 3.3 Application design for DEM

### 319 3.3.1 Communication information in each learning system

320 As shown in Fig. 4, all the agents will communicate with the microgrid EMS, in which each agent will transmit its current  
 321 optimal energy output or demand to the microgrid EMS. For the complex optimization subtask, the microgrid EMS is regarded  
 322 as an external environment for each learning agent, thus each agent can acquire the state and feedback reward after  
 323 implementing an optimal CE action. Besides, each learning agent can access the current actions and knowledge matrices of other  
 324 agents at any time. For the simple optimization subtask, the microgrid EMS will continuously issue the energy mismatches to

325 each agent, thus the consensus collaboration among the agents can be achieved.

### 326 3.3.2 Design of feedback reward

327 To maximize the social welfare, the feedback reward should be designed to match the total operating cost  $f_{\text{cost}}$  in (8), i.e., a  
328 smaller  $f_{\text{cost}}$  encourages a larger feedback reward, which can be calculated as follows:

$$329 R_j(s_k, \bar{a}) = C_1 - \left( f_j(x_j^k) + \frac{1}{J} \sum_{p=1, p \neq j}^N f_p(x_p^k) \right) / C_2 \quad j=1, 2, \dots, J \quad (46)$$

330 where  $f_j$  is the operating cost of the  $j$ th learning agent;  $C_1$  and  $C_2$  are the feedback reward coefficients.

### 331 3.3.3 Execution procedure

332 In summary, the CPSS with parallel learning for DEM of a microgrid is given in Fig. 6. Note that the convergence criteria of  
333 adaptive consensus algorithm is that both the electricity and heat energy mismatches ( $\Delta E$  and  $\Delta H$ ) can simultaneously satisfy the  
334 energy mismatch tolerance  $\tau$ , i.e., i.e.,  $|\Delta E| < \tau$  &  $|\Delta H| < \tau$ , where  $\tau$  is set to be 0.0001 in this paper. Beside, each agent will prefer to  
335 produce a decision behavior from (20)-(23) based on a probability distribution, which is set to be [0.7, 0.1, 0.1, 0.1] for  
336 utilitarian, egalitarian, plutocratic, and dictatorial, respectively.

## 337 4. Case studies

### 338 4.1 Simulation model

339 For the microgrids, the best available energy system should be selected, capable of satisfying the demand requirements for a  
340 particular area. During this process, the design engineers need to determine the optimal generation units selection, sizing, and  
341 siting for the microgrid. It is usually built with a minimization of planning cost under various constraints [40], such as technical,  
342 environmental, geographical, social and regulatory constraints. In order to obtain the optimal planning scheme, various  
343 optimization technique can be used for handling this problem. Since this paper mainly focuses on the microgrid operation rather  
344 than the microgrid planning, the testing system simply consults from the built microgrid in [19] and [41].

345 The testing microgrid is operated in grid-connected mode, which contains 11 energy suppliers, 7 energy demanders, where  
346 the suppliers consists of 3 PV units, 2 WTs, 2 DGs, 2 CHPs, 1 heat-only unit, and the main grid, as shown in Fig. 7. Besides, the  
347 complex optimization subtask is composed of tie-line power and the heat energy outputs of CHP units, while the simple  
348 optimization subtask consists of the rest controllable variables. The main parameters of testing microgrid are given in Tables 1  
349 to 6 and Figs. 7-8. In particular,  $\text{CHP}_1$  is enclosed by the two segment shape in Fig. 2, where the boundary nodes ABCDEF are  
350 (0, 1), (0.15, 1), (0.6, 0.85), (0.3, 0.05), (0.08, 0.2), and (0, 0.2), respectively. Besides,  $\text{CHP}_2$  is enclosed by the one segment  
351 shape with the boundary nodes ABCD, which are (0, 0.6), (0.6, 0.5), (0.35, 0.05), and (0, 0.1), respectively. Furthermore, the  
352 switching cyber connection is designed around the heat unit ( $\text{Heat}_1$ ), i.e., if  $\Delta E \cdot \Delta H \geq 0$ , then  $\text{Heat}_1$  will simultaneously connect  
353 with  $L_1$ ,  $L_2$ , and  $\text{DG}_1$ , otherwise,  $\text{Heat}_1$  will disconnect with them, while  $L_1$  and  $L_2$  will connect with each other. To construct the

354 human participations in real-world system, thirteen experimenters are employed as the controllers for each energy supplier or  
 355 demander, respectively. Through trial-and-error, the main parameters of parallel learning are given in Table 7.

356 In order to verify the performance of the proposed technique, four commonly used heuristic algorithms are introduced for  
 357 comparisons, including genetic algorithm (GA) [42], particle swarm optimization (PSO) [43], artificial bee colony (ABC) [44],  
 358 group search optimizer (GSO) [45], where population size and maximum iteration number are set to be 50 and 250, respectively.  
 359 Moreover, all the simulations are undertaken in Matlab R2016a by a small server with Intel(R) Xeon (R) E5-2670 v3 CPU at 2.3  
 360 GHz with 64 GB of RAM.

#### 361 *4.2 Study of convergence*

362 Figs. 9-11 provide the convergence of parallel learning under scenario 3 (at 14:00) with peak price, where the number of  
 363 VASs is set to be 5. It can be found from Fig. 10 that each system can converge to a high-quality optimal solution with a lower  
 364 total operating cost via an effective interaction with other systems, especially for the real-world system. At the same time, three  
 365 energy suppliers (tie-line power, CHP<sub>1</sub>, and CHP<sub>2</sub>) can achieve an optimal CE among them after around 200 CE based game  
 366 iterations, while the feedback reward of each one will increase as its energy output decrease and vice versa, as illustrated in Fig.  
 367 10. After each game iteration, twelve energy agents (suppliers and demanders) will interact their incremental costs for reaching a  
 368 consensus by adaptive consensus algorithm. As shown in Fig. 11(a), the interactive incremental cost will update between unified  
 369 consensus mode and independent consensus mode according to the dynamic energy mismatches, in which the heat-only unit  
 370 Heat<sub>1</sub> cannot reach a consensus with other electricity energy agents due to the heat energy balance constraint (10). Besides, the  
 371 actual incremental costs of some energy agents have reached their limits after a fewer interactions, thus their energy outputs or  
 372 responding power can strictly satisfy their capacity lower and upper limits, as shown in Fig. 11(b)-(e). Finally, both the  
 373 electricity and heat energy mismatches ( $\Delta E$  and  $\Delta H$ ) simultaneously satisfy the energy mismatch tolerance after a series of  
 374 corrections (See Fig. 11(f)), i.e.,  $|\Delta E| < \tau$  and  $|\Delta H| < \tau$ .

#### 375 *4.3 Comparative results and discussions*

376 Fig. 12 shows the convergence of total operating costs obtained by different algorithms under scenario 3. It is clear that both  
 377 parallel learning and PSO outperform other three algorithms because each of them can obtain a lower total operating cost in a  
 378 fewer iterations. Moreover, the detailed optimal dispatch strategies of all the energy suppliers and demanders obtained by  
 379 different algorithms are listed in Table 8. It verifies that the proposed parallel learning can not only realize the distributed  
 380 optimization of DEM with human participation and interaction, but also can guarantee the quality of the obtained optimal  
 381 solution compared with the commonly used centralized heuristic algorithms, which results from the deep exploitations and  
 382 explorations with various decision strategies (20)-(23) in multiple VASs.

383 In order to further test the performance of parallel learning, all the algorithms are implemented for three different scenarios  
384 (See Table 6) with 50 independent runs. Fig. 13 shows the statistical results obtained by them, where parallel learning I, parallel  
385 learning II, and parallel learning III represent the parallel learning with different numbers of VASs, i.e., 5, 10, and 15  
386 respectively. It also proves that parallel learning can search the highest quality optimal solution with a lowest total operating cost  
387 under each scenario, especially parallel learning with more VASs. This obviously demonstrates that the increasing VASs can  
388 generate a potential higher quality optimal solution via a deeper exploitation and exploration with various decision strategies.  
389 However, it requires more computation capability and consumes more execution time, as shown in Fig. 13(d). Furthermore, the  
390 execution time of parallel learning is slightly larger than that of GA, PSO, and GSO since each game agent requires a linear  
391 programming computation to search an optimal CE policy at each iteration.

#### 392 *4.4 Study of influence by renewables uncertainty*

393 For the DEM of a microgrid, the uncertainty of the input parameters is ubiquitous due to the unavoidable forecast error,  
394 especially for the intermittent energy out of renewables. In order to figure out the influence by the renewables uncertainty, Fig.  
395 14 provides the statistical results obtained by proposed system under different uncertainty degrees in 50 runs, where the  
396 uncertainty degree represent the forecast error of the total energy output of renewables; both the total operating cost and the  
397 execution time are the average of 50 runs. It is clearly that the obtained total operating cost decreases as the forecast error  
398 increases under each scenario, which results from that a larger energy output of renewables is beneficial to reduce the fuel cost  
399 of the microgrid. On the other hand, the execution time of parallel learning is almost not affected by the renewable uncertainty  
400 (See Fig. 14(d)), which also verifies the high convergence stability of the proposed method. Moreover, there is only little  
401 difference on the total operating costs obtained among all the parallel learning with different numbers of VASs. This reveals that  
402 the testing microgrid only requires a small number of VASs for parallel learning based DEM.

## 403 **6. CONCLUSION**

404 In this paper, a novel CPSS with parallel learning has been proposed for DEM of a microgrid. The main contributions can be  
405 summarized as follows

406 (i) The proposed CPSS is constructed by considering the human participation and interaction in social space, which can  
407 widely yield potential optimal distributed strategies for DEM in a real-world microgrid.

408 (ii) The CE based human interaction with various decision strategies can efficiently search an optimal dispatch strategy of a  
409 complex optimization subtask of DEM, including the tie-line power with a nondifferentiable objective function, and the CHP  
410 units with complex feasible operating regions constraints.

411 (iii) The adaptive consensus algorithm based human interaction can effectively achieve the self-organization of each human

with local communications, while the switch between unified consensus and independent consensus can simultaneously satisfy the consensus requirement and the multi-energy balance constraints.

(iv) The real-world system can continuously learn the knowledge from multiple virtual VASs, in which a deep exploitation and exploration can be implemented in each VAS. Hence, the quality of the obtained optimal solution of DEM can be guaranteed for the real-world system without any adverse trials, i.e., a lower total operating cost (higher social welfare) of a microgrid can be obtained.

(v) The proposed CPSS with parallel learning is not only highly independent on the mathematical model for a specific optimization, but also can achieve a high-quality optimum in a distributed manner. Hence, it can also be applied to other optimizations of the complex energy system.

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509 **Table 1**

510 Parameters of renewable energy resources.

WT		PV	
$v_{in}$	4 m/s	$S_{ref}$	1000 W/m <sup>2</sup>
$v_{out}$	25 m/s	$T_{ref}$	25°C
$v_r$	15 m/s	$\alpha_{pv}$	-0.47%/°C
Rated power	0.5 MW	Rated power	0.5 MW

511 **Table 2**

512 Parameters of DGs and heat-only units.

Units	Operating cost coefficients			Capacity (MW)	
	$\alpha_i$	$\beta_i$	$\gamma_i$	Minimum	Maximum
DG <sub>1</sub>	10.193	210.36	250.2	0	0.5
DG <sub>2</sub>	2.305	301.4	1100	0.04	0.2
Heat <sub>1</sub>	33	12.3	6.9	0	2

513 **Table 3**

514 Operating cost coefficients of CHP units.

Units	$\alpha_i$	$\beta_i$	$\gamma_i$	$\delta_i$	$\theta_i$	$\zeta_i$
CHP <sub>1</sub>	339.5	185.7	44.2	53.8	38.4	40
CHP <sub>2</sub>	100	288	34.5	21.6	21.6	8.8

515 **Table 4**

516 Electricity buying and selling prices from the main grid.

Tariff type	Time	Buying price (\$/MWh)	Selling price (\$/MWh)
Tariff 1 (low price)	00:00—06:59	192	180
Tariff 2 (shoulder price)	07:00—10:59	238	200
	16:00—18:59		
Tariff 3 (peak price)	22:00—23:59	317	260
	11:00—15:59		
	19:00—21:59		

517 **Table 5**

518 Operating cost coefficients of linear demand versus price expression at different tariffs.

Demanders	Tariff 1		Tariff 2		Tariff 3	
	$a^{lin}$	$b^{lin}$	$a^{lin}$	$b^{lin}$	$a^{lin}$	$b^{lin}$
L <sub>1</sub>	0.9	-0.0028	0.95	-0.0025	1	-0.002
L <sub>2</sub>	0.9	-0.0028	0.95	-0.0025	1	-0.002
L <sub>3</sub>	0.9	-0.0025	0.95	-0.002	1	-0.001
L <sub>4</sub>	0.9	-0.0025	0.95	-0.002	1	-0.001
L <sub>5</sub>	0.9	-0.0025	0.95	-0.002	1	-0.001
L <sub>6</sub>	0.9	-0.0042	0.95	-0.004	1	-0.0035
L <sub>7</sub>	0.9	-0.0042	0.95	-0.004	1	-0.0035

519 **Table 6**

520 Forecasting results of energy demand and renewable energy outputs under three scenarios.

Demanders or renewables	Energy type	Forecasting results (MW)		
		Scenario 1 (00:00)	Scenario 2 (09:00)	Scenario 3 (14:00)
L <sub>1</sub>	Electricity	0.13	0.38	0.5
	Heat	0.04	0.04	0.03
L <sub>2</sub>	Electricity	0.12	0.33	0.4
	Heat	0.03	0.03	0.03
L <sub>3</sub>	Electricity	0.14	0.42	0.6
	Heat	0.05	0.04	0.04

L <sub>4</sub>	Electricity	0.19	0.38	0.45
	Heat	0.05	0.04	0.03
L <sub>5</sub>	Electricity	0.2	0.44	0.55
	Heat	0.06	0.04	0.04
L <sub>6</sub>	Electricity	0.26	0.4	0.5
	Heat	0.07	0.04	0.04
L <sub>7</sub>	Electricity	0.07	0.18	0.35
	Heat	0.02	0.02	0.02
PV <sub>1</sub>	Electricity	0	0.02	0.1
PV <sub>2</sub>	Electricity	0	0.01	0.1
PV <sub>3</sub>	Electricity	0	0.02	0.1
WT <sub>1</sub>	Electricity	0.28	0.25	0.2
WT <sub>2</sub>	Electricity	0.36	0.32	0.3

521 **Table 7**

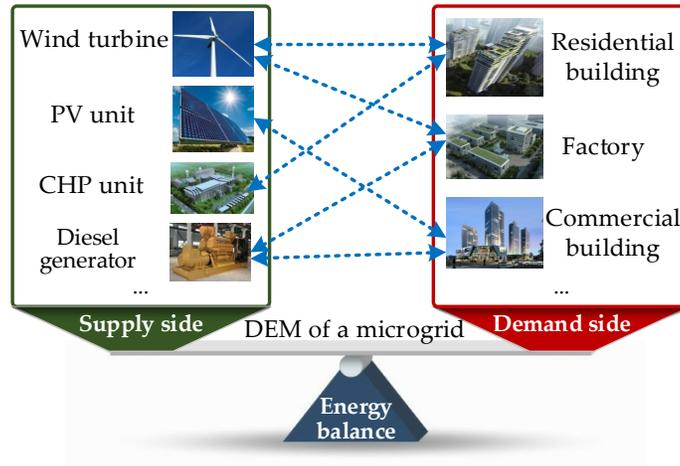
522 The main parameters of parallel learning.

Parameter	Range	Value
$\alpha$	$0 < \alpha < 1$	0.9
$\gamma$	$0 < \gamma < 1$	0.1
$\varepsilon$	$0 < \varepsilon < 1$	0.9
$\mu$	$\mu > 0$	3
$C_p$	$0 < C_p < 1$	0.9
$C_1$	$C_1 > 0$	1
$C_2$	$C_2 > 0$	1000
$k_{\max}$	$k_{\max} > 0$	250

523 **Table 8**

524 Comparative results of optimal solutions obtained by different algorithms under scenario 3.

Demanders or Suppliers	Energy type	Optimal energy generations and consumptions (MW)				
		GA	PSO	ABC	GSO	Parallel learning
L <sub>1</sub>	Electricity	0.419	0.410	0.422	0.432	0.412
	Heat	0.030	0.030	0.030	0.030	0.030
L <sub>2</sub>	Electricity	0.371	0.357	0.344	0.385	0.362
	Heat	0.030	0.030	0.030	0.030	0.030
L <sub>3</sub>	Electricity	0.597	0.600	0.581	0.600	0.600
	Heat	0.040	0.040	0.040	0.040	0.040
L <sub>4</sub>	Electricity	0.448	0.450	0.409	0.450	0.450
	Heat	0.030	0.030	0.030	0.030	0.030
L <sub>5</sub>	Electricity	0.540	0.550	0.542	0.550	0.550
	Heat	0.040	0.040	0.040	0.040	0.040
L <sub>6</sub>	Electricity	0.451	0.450	0.461	0.454	0.450
	Heat	0.040	0.040	0.040	0.040	0.040
L <sub>7</sub>	Electricity	0.279	0.270	0.282	0.270	0.270
	Heat	0.020	0.020	0.020	0.020	0.020
PV <sub>1</sub>	Electricity	0.100	0.100	0.100	0.100	0.100
PV <sub>2</sub>	Electricity	0.100	0.100	0.100	0.100	0.100
PV <sub>3</sub>	Electricity	0.100	0.100	0.100	0.100	0.100
WT <sub>1</sub>	Electricity	0.200	0.200	0.200	0.200	0.200
WT <sub>2</sub>	Electricity	0.300	0.300	0.300	0.300	0.300
Tie-line power	Electricity	0.355	0.399	0.387	0.399	0.399
DG <sub>1</sub>	Electricity	0.325	0.248	0.261	0.308	0.255
DG <sub>2</sub>	Electricity	0.040	0.040	0.096	0.041	0.040
CHP <sub>1</sub>	Electricity	0.993	1.000	0.923	0.999	1.000
	Heat	0.009	0.000	0.047	0.001	0.000
CHP <sub>2</sub>	Electricity	0.591	0.600	0.573	0.594	0.599
	Heat	0.026	0.000	0.152	0.015	0.000
Heat <sub>1</sub>	Heat	0.195	0.230	0.031	0.215	0.226
Total operating cost $f_{\text{cost}}$ (\$/h)		1182.886	1176.073	1210.318	1178.385	<b>1176.021</b>

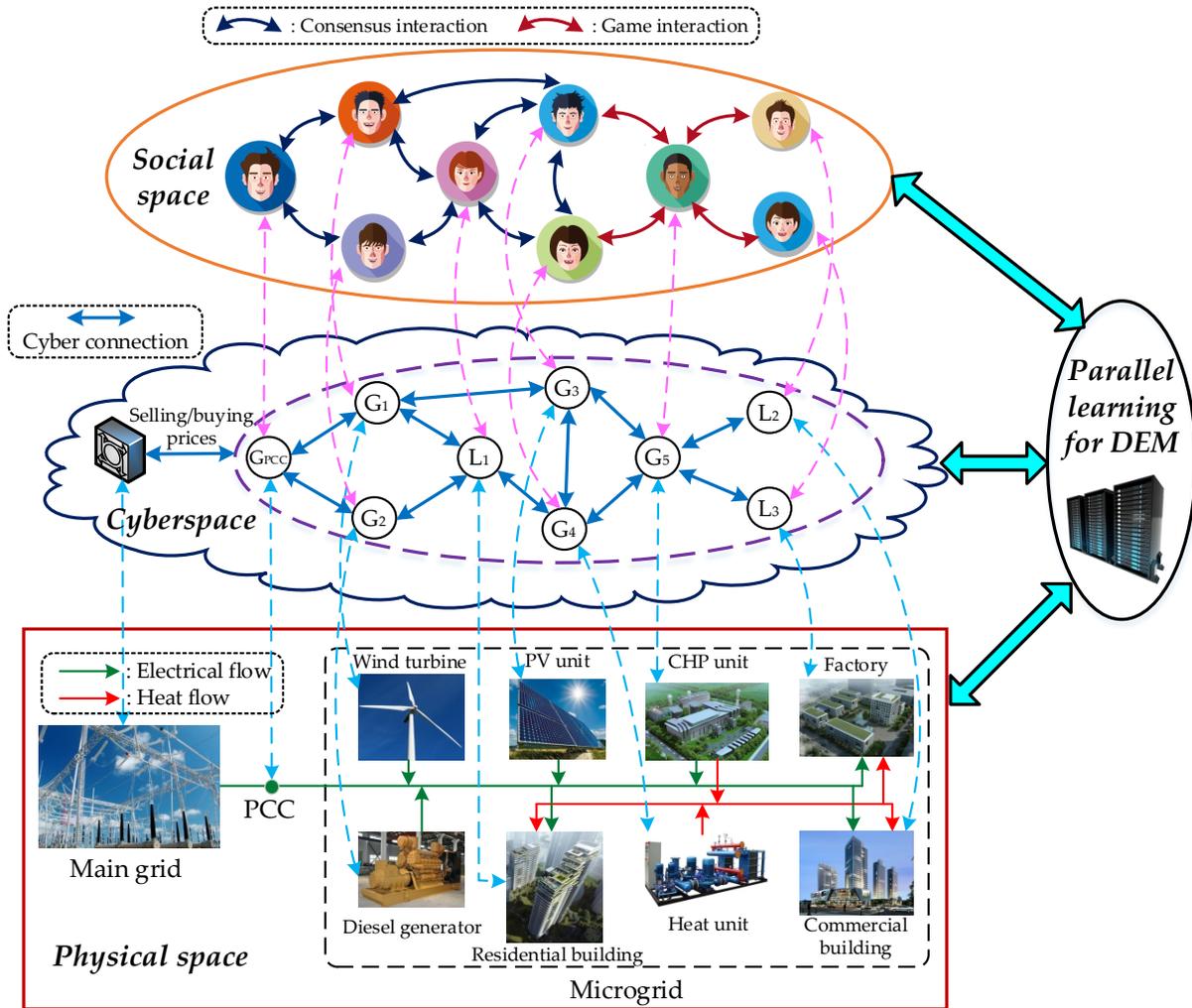


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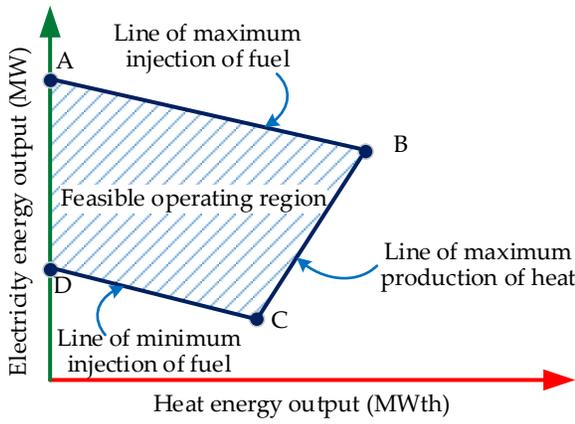
Fig. 1 DEM of a microgrid with different units.



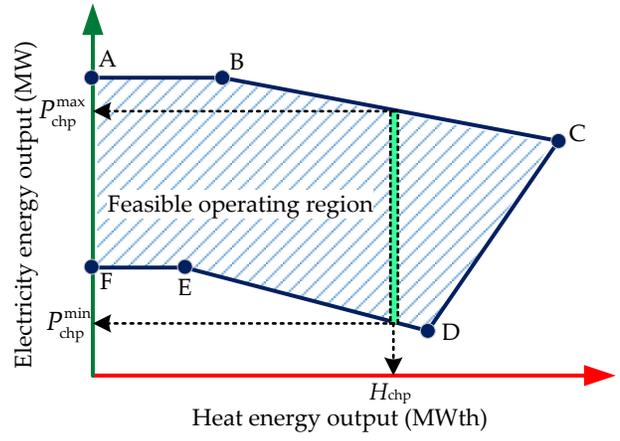
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Fig. 3 CPSS framework for DEM of a microgrid.



(a) One segment shape



(b) Two segment shape

Fig. 2 Feasible operating region of CHP units.

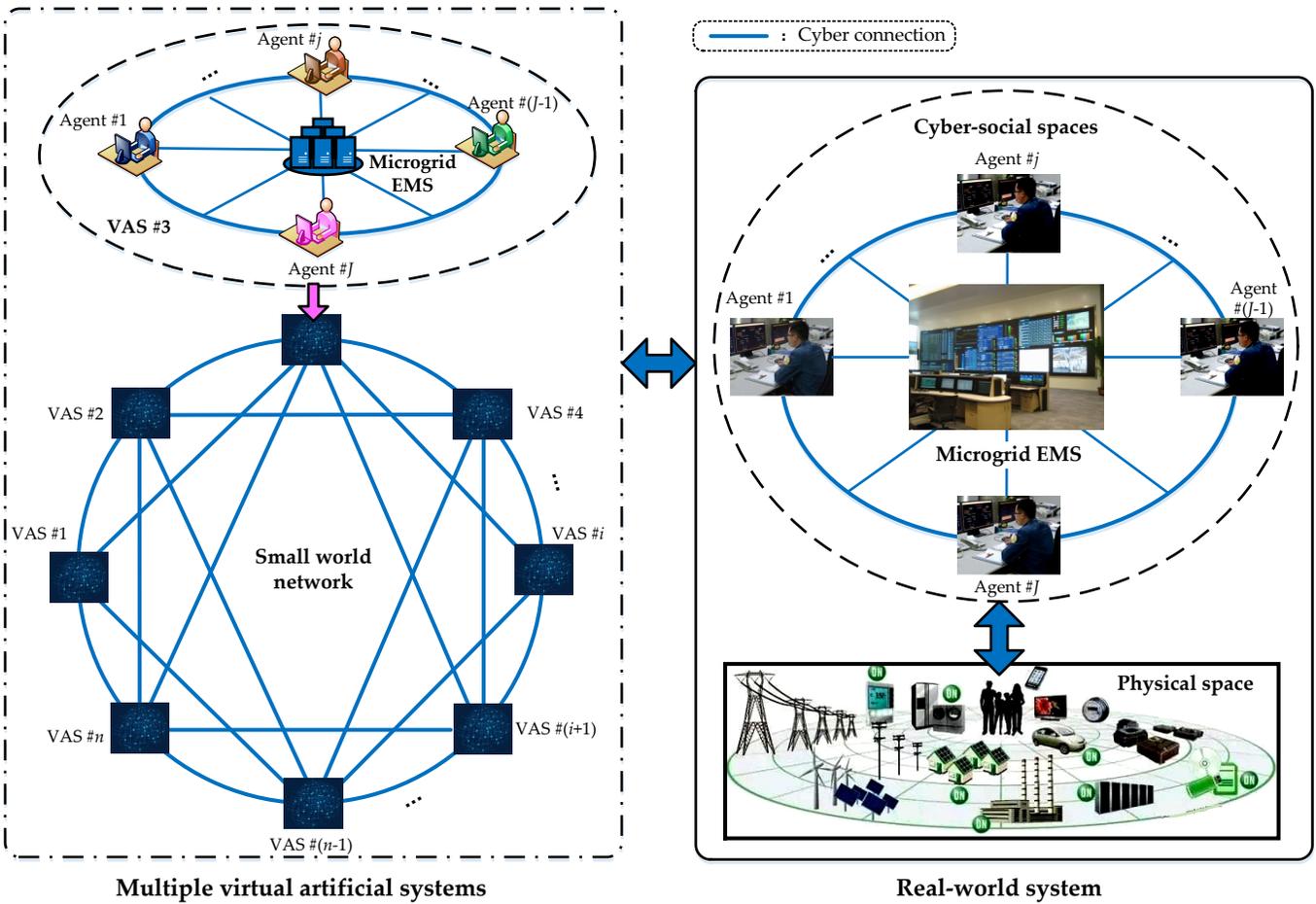


Fig. 4 Parallel learning with multiple virtual artificial systems and a real-world system.

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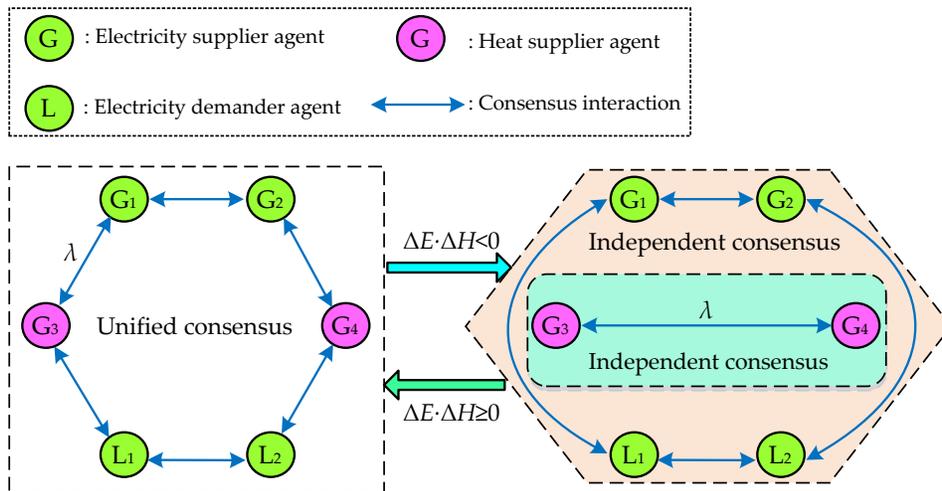


Fig. 5 Principle of human interaction by adaptive consensus algorithm.

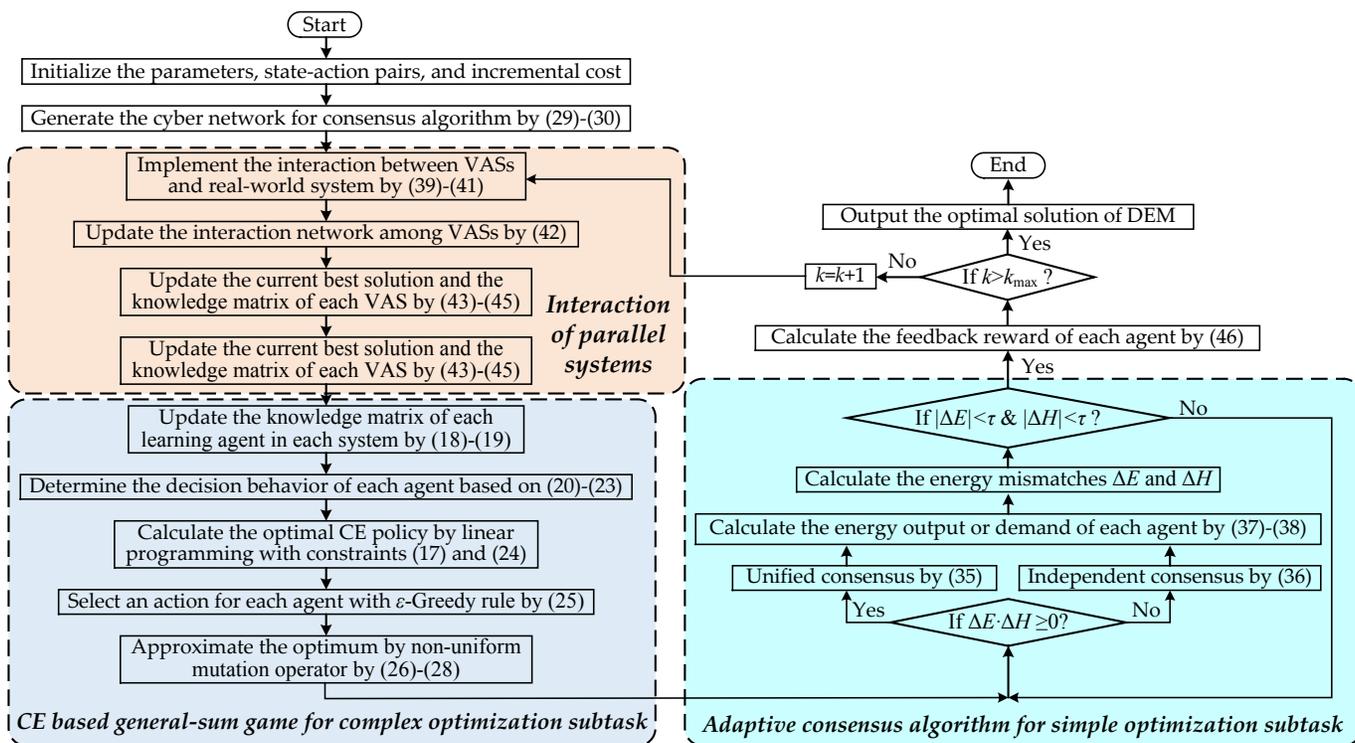
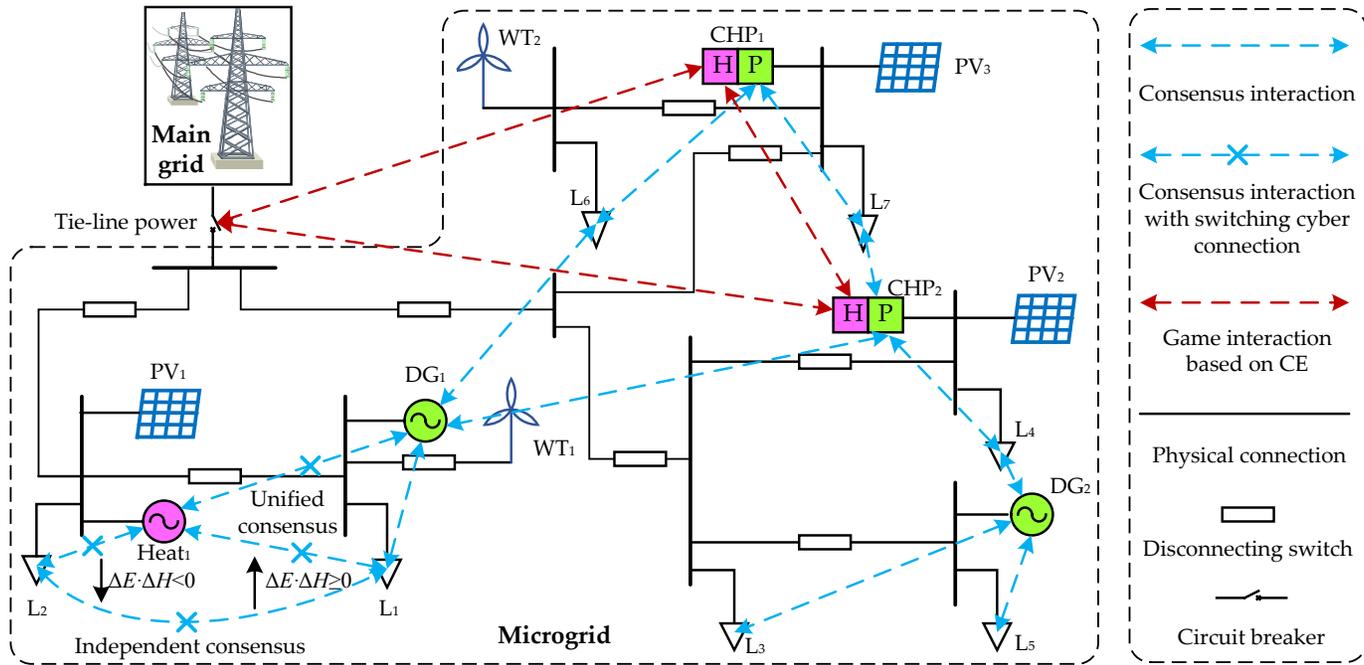


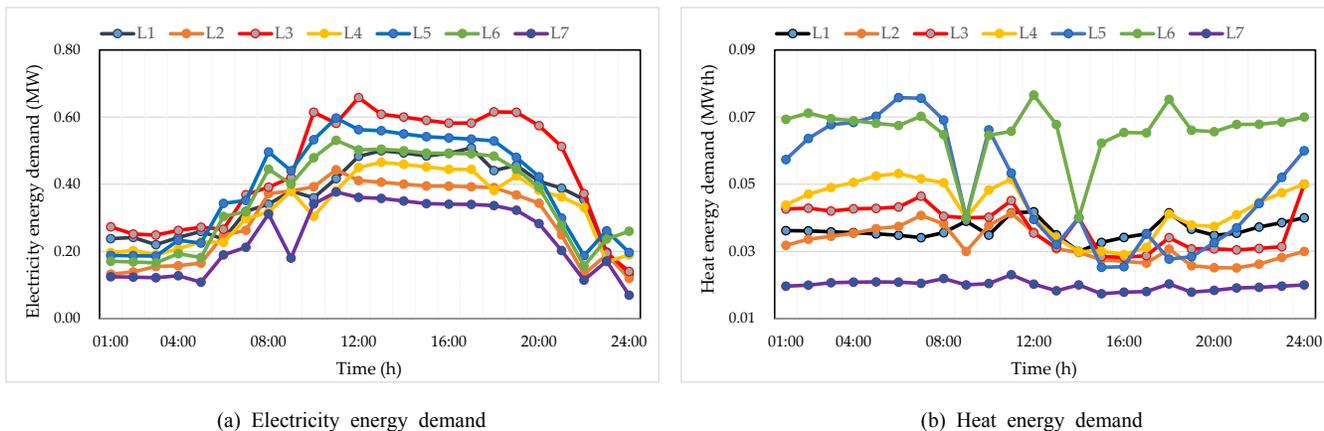
Fig. 6 Execution procedure of CPSS with parallel learning for DEM of a microgrid.



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Fig. 7 CPSS of the testing microgrid.

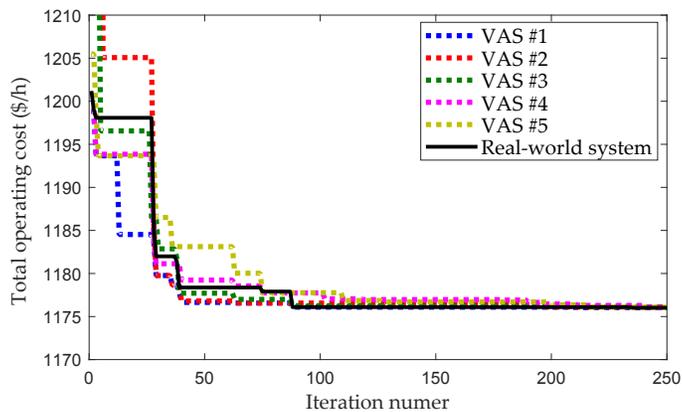


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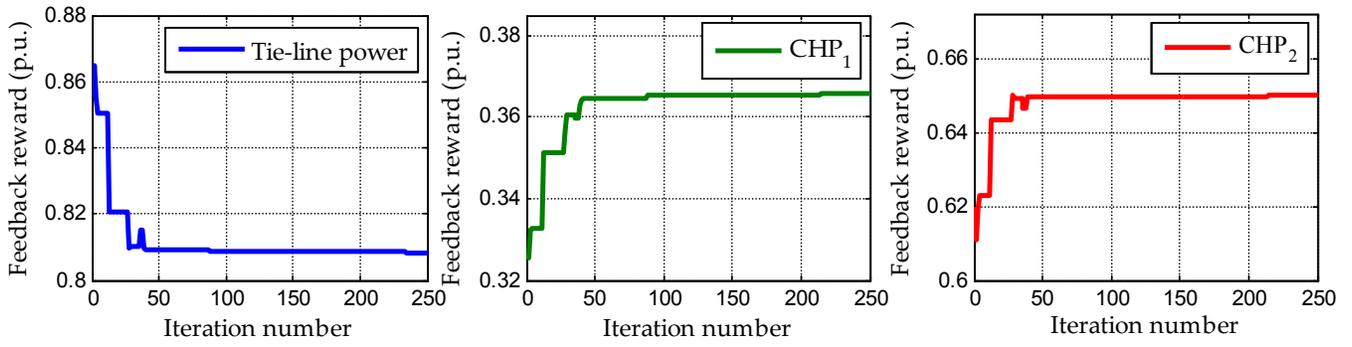
Fig. 8 Energy demand profiles of energy demanders in a day.



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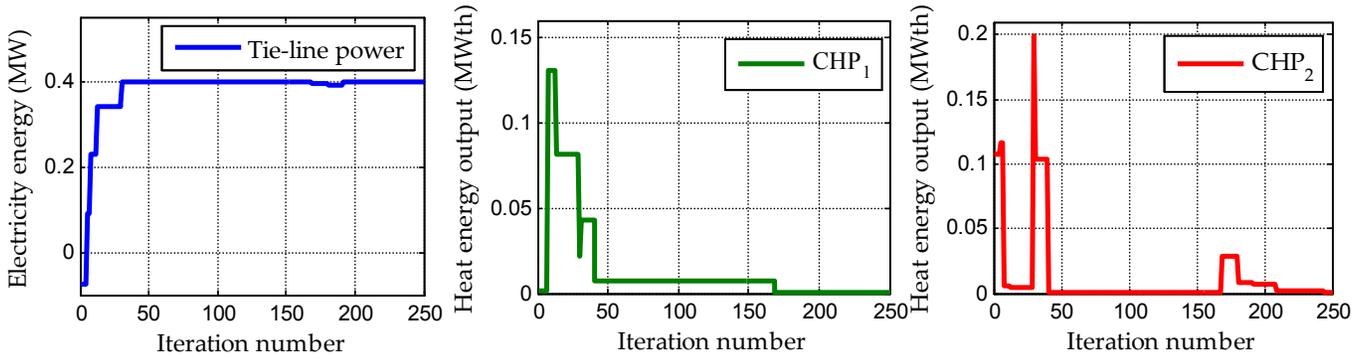
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Fig. 9 Convergence of parallel learning in different systems.



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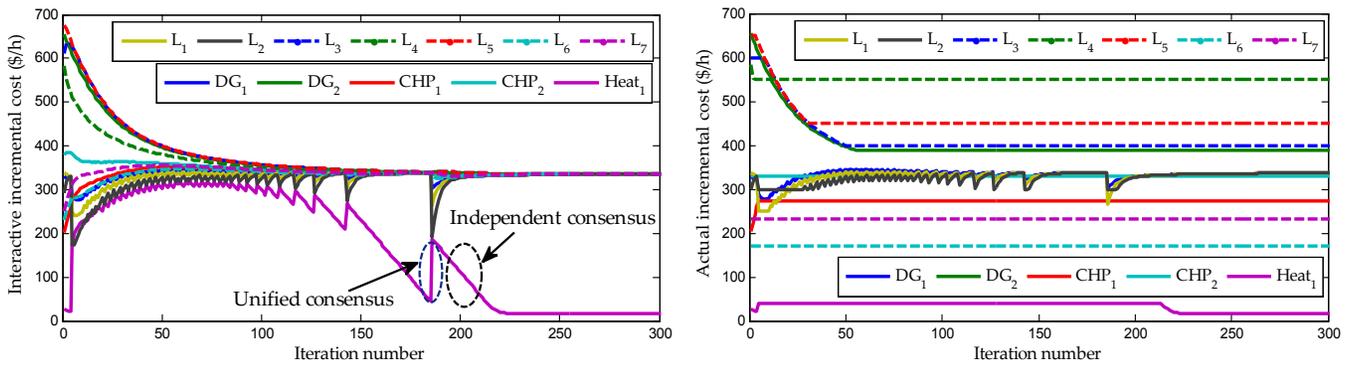
(a) Convergence of feedback reward



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(b) Convergence of energy output

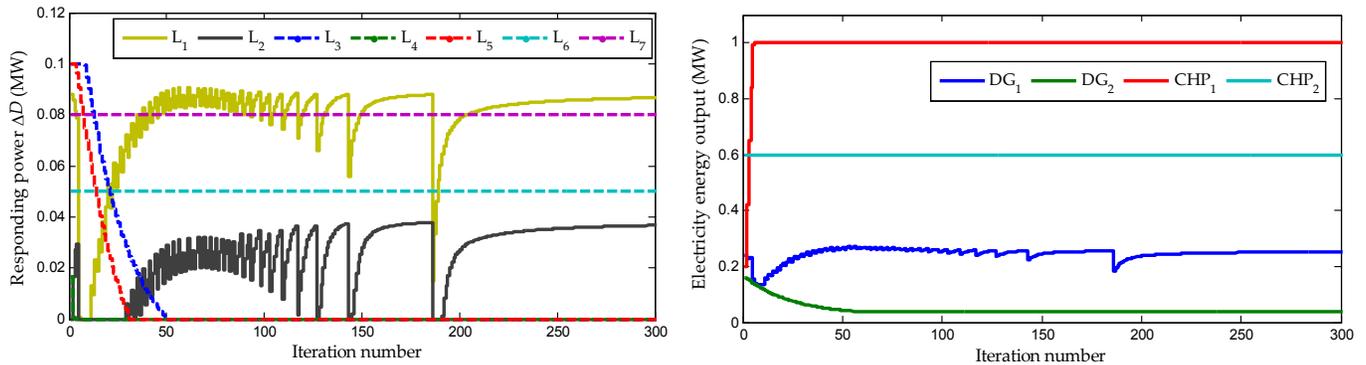
**Fig. 10** Convergence of CE based human interaction in the real-world system.



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(a) Convergence of interactive incremental cost

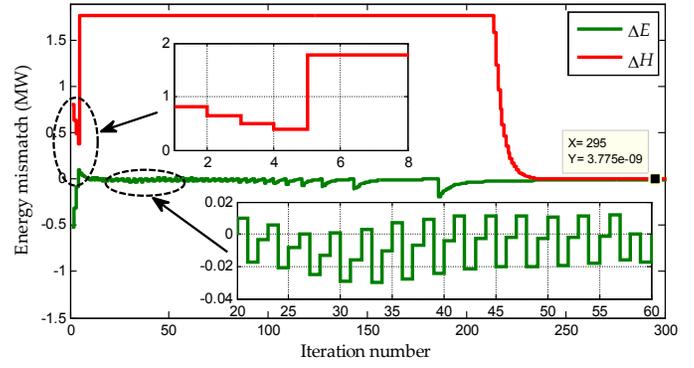
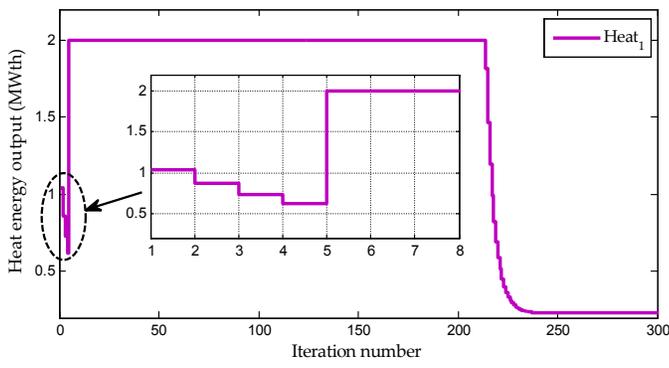
(b) Convergence of actual incremental cost



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(c) Convergence of responding power of different energy demanders

(d) Convergence of electricity energy output



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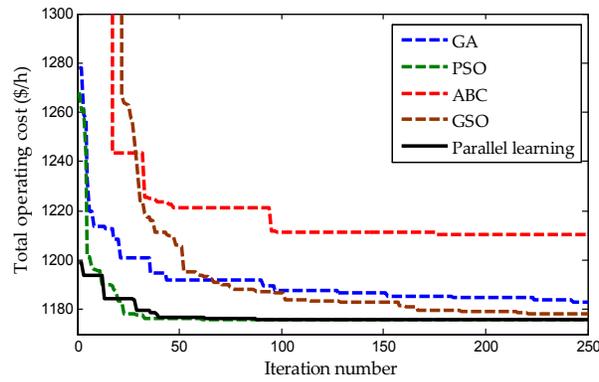
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(e) Convergence of heat energy output

(f) Convergence of energy mismatches

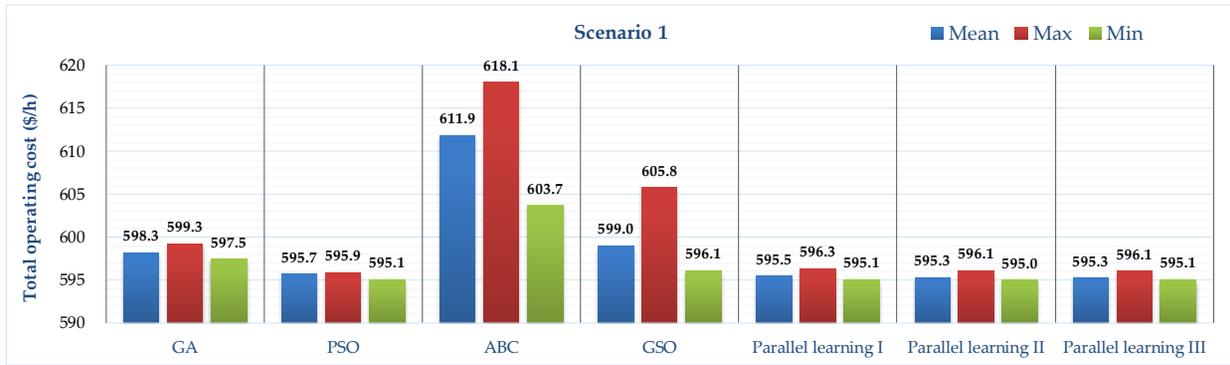
**Fig. 11** Convergence of adaptive consensus algorithm based human interaction in the real-world system at the final game iteration.



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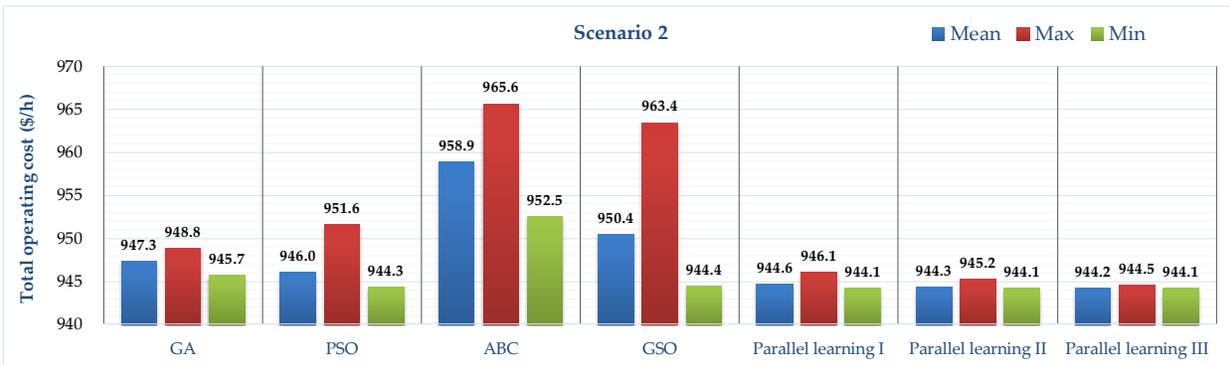
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**Fig. 12** Convergence of total operating costs obtained by different algorithms under scenario 3.



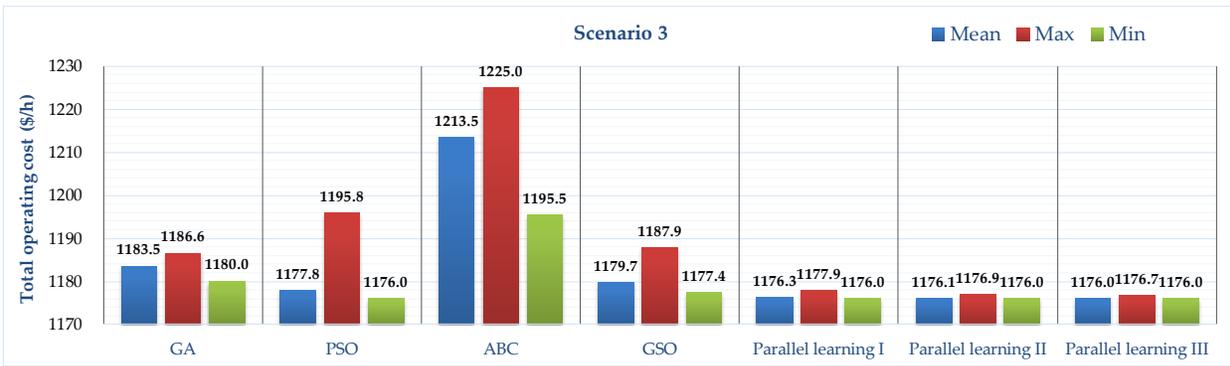
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(a) Obtained total operating costs under scenario 1



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(b) Obtained total operating costs under scenario 2



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(c) Obtained total operating costs under scenario 3

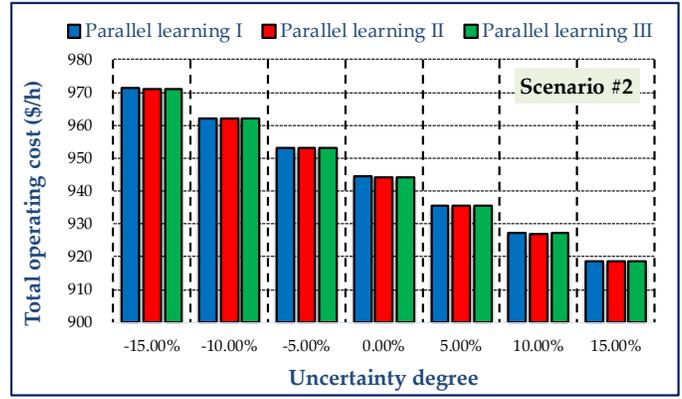
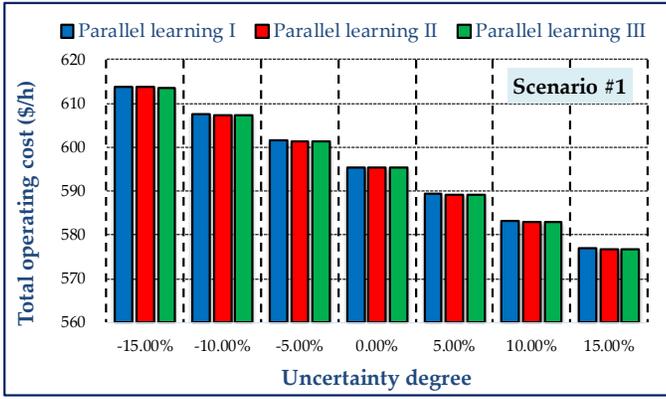


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(d) Execution time of each scenario

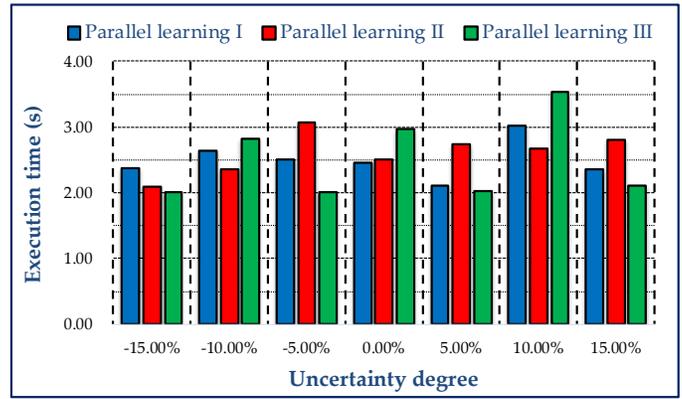
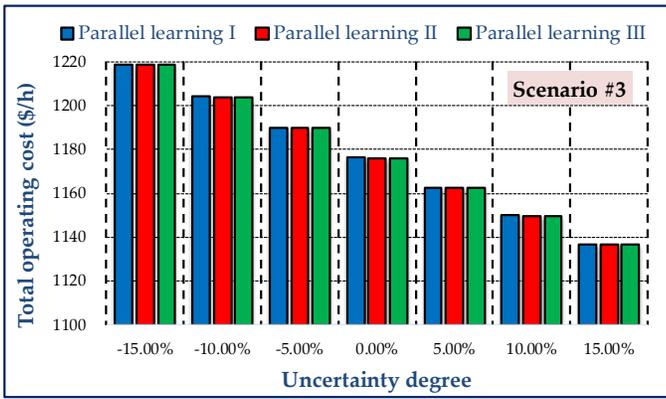
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Fig. 13 Statistical results obtained by different algorithms under three scenarios in 50 runs.



(a) Obtained total operating costs under scenario 1

(b) Obtained total operating costs under scenario 2



(c) Obtained total operating costs under scenario 3

(d) Execution time of each scenario

Fig. 14 Statistical results obtained by CPSS with parallel learning under different uncertainty degrees in 50 runs.

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- *A cyber-physical-social system is constructed for distributed energy management.*
- *A game theory with various decision behaviors is proposed for human interaction.*
- *Energy suppliers or demanders can reach a consensus on the incremental cost.*
- *The parallel interactive systems can lead to a lower total operating cost.*
- *The proposed method outperforms other centralized heuristic algorithms for DEM.*